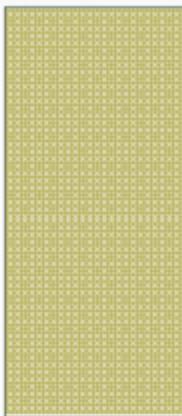


6.6

GENERAL FORM OF THE EQUATION FOR A LINEAR
RELATION



GENERAL FORM

General Form of the Equation of a Linear Relation

$Ax + By + C = 0$ is the general form of the equation of a line, where A is a whole number, and B and C are integers.

- # A, B, C cannot be fractions ~~or~~
- * A must be positive ~~*~~

EX 1 REWRITING AN EQUATION IN GENERAL FORM

a)
$$\left(y = -\frac{2}{3}x + 4 \right)$$
 ← make this \emptyset

$$3y = -2x + 12$$

$$3y - 12 = -2x$$

$$2x + 3y - 12 = 0 \checkmark$$

EX 1 CONTINUED

b) $y - 1 = \frac{3}{5}(x + 2)$ \uparrow make this
 \emptyset

$$5y - 5 = 3(x + 2)$$

$$5y - 5 = 3x + 6$$

$$5y - 11 = 3x - 3x$$

$$-1(-3x + 5y - 11) = 0 \quad \leftarrow \text{to get rid of } -A,$$

$$3x - 5y + 11 = 0 \quad \checkmark \quad \begin{matrix} \text{multiply everything by a} \\ -1. \end{matrix}$$

YOUR TURN

a) $y = -\frac{1}{4}x + 3$

b) $y + 2 = \frac{3}{2}(x - 4)$

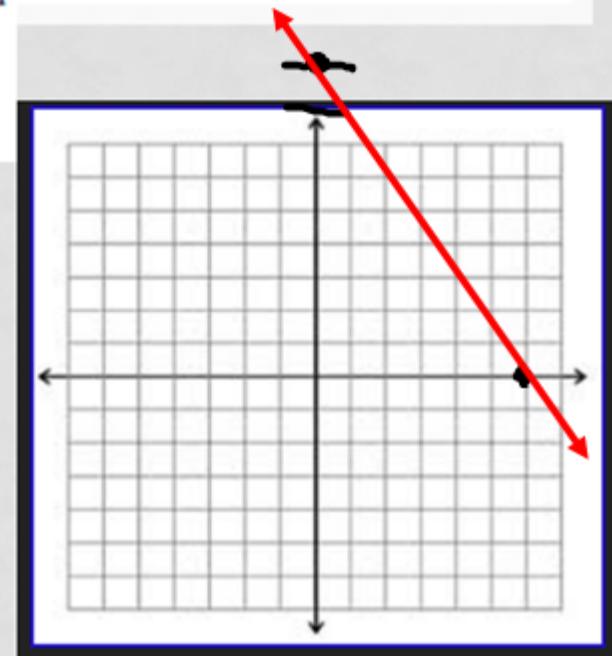
EX 2 - GRAPHING A LINE IN GENERAL FORM

- a) Determine the x- and y-intercepts of the line whose equation is: $3x + 2y - 18 = 0$

b) Graph the line.

$$\begin{aligned}
 & \frac{x\text{-int}}{\text{Set } y=0} \\
 & 3x - 18 = 0 \\
 & 3x = \frac{18}{3} \\
 & x = 6 \\
 & (6, 0)
 \end{aligned}$$

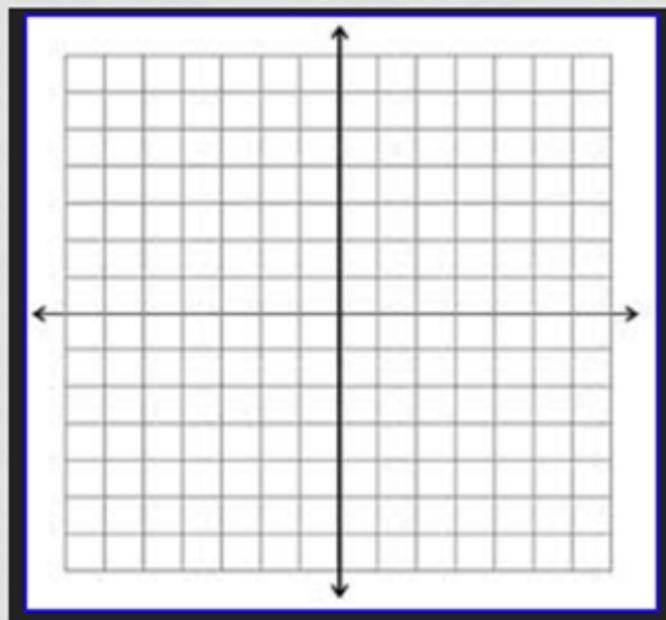
$$\begin{aligned}
 & \frac{y\text{-int}}{\text{Set } x \text{ to } 0} \\
 & 2y - 18 = 0 \\
 & 2y = \frac{18}{2} \\
 & y = 9 \\
 & (0, 9)
 \end{aligned}$$



$$\begin{aligned}
 & \frac{x\text{-int}}{(x, 0)} \\
 & \frac{y\text{-int}}{(0, y)}
 \end{aligned}$$

YOUR TURN

- a) Determine the x - and y -intercepts of the line whose equation is:
$$x + 3y + 9 = 0$$
- b) Graph the line.



EX 3 - DETERMINE SLOPE, GIVEN EQUATION IN GENERAL FORM

Determine the slope of the line with this equation:

$$3x - 2y - 16 = 0 \quad +16 \quad +16$$

Slope-int. form

$$\begin{aligned} & \cancel{3x} \\ 3x - 2y &= 16 - \cancel{3x} \quad \text{Algebraic order} \\ \cancel{2y} &= -3x + 16 \\ \frac{1}{2}y &= -\frac{3}{2}x + 8 \end{aligned}$$

$$y = \frac{3}{2}x - 8$$

m

Slope = $\frac{3}{2}$

YOUR TURN

Determine the slope of the line
with this equation:

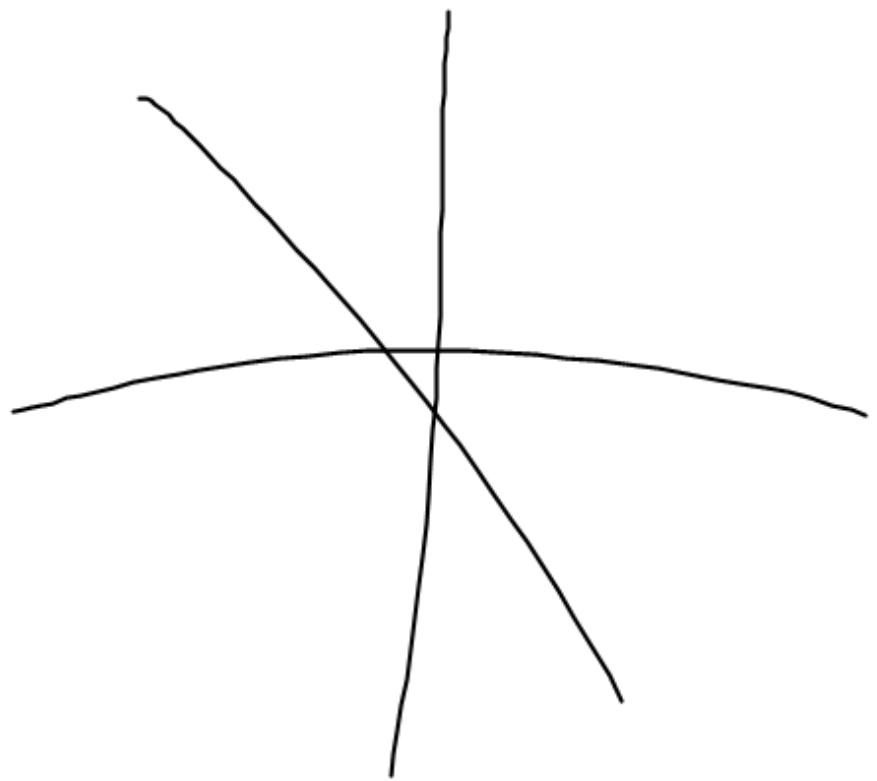
$$5x - 2y + 12 = 0 \quad \leftarrow \text{change to slope-int. form}$$

$$\frac{-5x}{-2} - 12 = -5x$$

$$\frac{-2y}{-2} = -5x - 12$$

$$y = \frac{5}{2}x + 6$$

Slope = $\frac{5}{2}$



ASSIGNMENT

- Page 384, 4-9,13,14,18
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4-9, 13, 14, 18